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NEON ALGORITHM THEORETICAL BASIS DOCUMENT: FREQUENCY RESPONSE CORRECTIONS FOR THE EDDY-COVARIANCE TURBULENT EXCHANGE SUBASSEMBLY

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TABLE OF CONTENTS

1	C	ESCRI	PTION	1
	1.1	Purp	ose	1
	1.2	Scop	e	1
2	R	ELATE	D DOCUMENTS	1
	2.1	Appl	icable documents	1
	2.2	Refe	rence documents	2
	2.3	Verb	convention	2
3	D	ESCRI	PTION OF VARIABLES	2
	3.1	Repo	orted variables	3
	3.2	Inpu	t variables	3
	3.3	Prod	luct instances	4
	3.4	Tem	poral resolution and extent	4
	3.5	Spat	ial resolution and extent	4
4	S	CIENTI	FIC CONTEXT	4
	4.1	Theo	ory of measurement/observation	4
	4.2	Theo	ory of algorithm	5
	4	.2.1	Wavelet-based spectral correction method	8
	4	.2.2	Discrete wavelet transform	9
	4	.2.3	Spectral peaks	11
	4	.2.4	Power law coefficient in the inertial subrange	11
	4	.2.5	Distribution of amplitude adjustment	12
	4	.2.6	Correction for high-frequency loss	12



Author: S. Metzger

Date: 08/02/2013

NEON.DOC.000854

Revision: A

	4.	2.7	Reconstruction of the corrected time series
5	Αl	.GOR	ITHM IMPLEMENTATION
6	UI	NCER	TAINTY
(6.1	Ana	lysis of uncertainty14
(6.2	Rep	orted uncertainty14
7	Αl	.GOR	ITHM VERIFICATION14
8	SC	CIENT	TIFIC AND EDUCATIONAL APPLICATIONS
9	FU	JTUR	E PLANS AND MODIFICATIONS15
10	Αſ	PPEN	DIX15
-	10.1	А	ocronyms15
-	10.2	F	unctions16
-	10.3	Р	Parameters
-	10.4	S	ubscripts17
-	10.5	٧	/ariables18
11	ВІ	BLIO	GRAPHY19
LIS	т о	F TA	BLES AND FIGURES
_			ormalized power spectrum for an ideal instrument which measures the unaffected spectrum
			ce, and for a non-ideal instrument6 verview of the wavelet-based spectral correction method for four case studies
_			lation of the resolution of location and scale for the discrete wavelet transform10
Tal	ble 1	L. List	of variables that are produced in this ATBD3
			of input variables that are used in this ATBD3



Author: S. Metzger

Date: 08/02/2013

NEON.DOC.000854

Revision: A

1 DESCRIPTION

NEON shall measure the exchange of momentum, energy and trace gases between the earth's surface and the atmosphere. To accomplish this, NEON will operate an eddy covariance turbulent exchange subsystem (EC-TES, a summary of all acronyms, functions, parameters and variables is provided in Sect. 10), which collectively embodies a suite of sensors.

1.1 Purpose

This document describes the theoretical background and entire algorithmic process for correcting the limited high-frequency response of outputs from EC-TES sensors. The present algorithm theoretical basis document (ATBD) serves to summarize all corresponding algorithms which will be used during the implementation of AD[01].

1.2 Scope

This ATBD is embedded in a suite of 29 existing and upcoming NEON documents, which collectively describe the acquisition, processing and quality control of data from the EC-TES (AD[01] provides an overview). As such, the scope of this ATBD is to provide all necessary processing steps between immediately preceding and succeeding documents. This ATBD first introduces related documents, acronyms and conventions (Sect. 2). Throughout Sects. 3–6, (i) all reported variables and input variables are identified, (ii) theoretical background is provided, (iii) explicit algorithm descriptions are given, and (iv) error propagation algorithms are provided that enable the calculation of uncertainty budgets for each reported variable. This document does not provide computational implementation details, except for cases where these stem directly from algorithmic choices explained here.

2 RELATED DOCUMENTS

2.1 Applicable documents

AD[01]	NEON.DOC.000573	FIU Plan for airshed QA/QC development
AD[02]	NEON.DOC.000853	Coordinate rotations ATBD
AD[03]	NEON.DOC.000823	Calculation of variances and covariances ATBD
AD[04]	NEON.DOC.000465	Eddy-covariance turbulent exchange subsystem C ³
AD[05]	NEON.DOC.000651	Atmospheric properties/units ATBD



Title: NEON Algorithm Theoretical Basis Do	ocument –
Frequency Response Corrections	

Date: 08/02/2013

NEON.DOC.000854

Revision: A

AD[06]	NEON.DOC.000822 Eddy-Covariance Storage Exchange ATBD	
AD[07]	NEON.DOC.001097 FFT/Wavelet Analysis/Spectral ATBD	
AD[08]	Freely available source code to Nordbo, A. & Katul, G. (2012) A wavelet-based correction method for eddy-covariance high-frequency losses in scalar concentration measurements. Boundary-Layer Meteorology, 146 , 81-102.	
AD[09]	NEON.DOC.000848 NEON Science Commissioning and Validation Plan	

2.2 Reference documents

RD[01]	NEON.DOC.000008	NEON Acronym List
RD[02}	NEON.DOC.000243	NEON Glossary of Terms

2.3 Verb convention

"Shall" is used whenever a specification expresses a provision that is binding. The verbs "should" and "may" express non-mandatory provisions. "Will" is used to express a declaration of purpose on the part of the design activity.

3 DESCRIPTION OF VARIABLES

The algorithms in this ATBD provide all necessary processing steps between immediately preceding and succeeding ATBDs in a suite of NEON documents related to the EC-TES (Sect. 1.2, AD[01]). In general, the input variables of this ATBD are generated in preceding EC-TES-related documents, and the reported variables are used in succeeding documents. Which of these variables will be mapped to NEON data products (DP), as well as their corresponding IDs will be defined in succeeding documents, and are not provided in this ATBD.



Title: NEON Algorithm The	eoretical Basis Document –
Eroquancy Paspansa Carra	ctions

Date: 08/02/2013

NEON.DOC.000854

Revision: A

3.1 Reported variables

Table 1 details the variables reported by the algorithms disclosed in this ATBD.

Table 1. List of variables that are produced in this ATBD.

Variable	Units
Time series (0.05 s temporal resolution) of atmospheric scalar, corrected for high-frequency loss (X_c)	Depending on scalar
One quality metric for X per averaging period, indicating whether high-frequency loss correction could be performed ($QM_{att} = 0\%$) or not ($QM_{att} = 100\%$).	%

3.2 Input variables

Table 2 lists all input variables that are used to produce the output variables reported above. The data sources and specific data product IDs will be provided in ATBDs that use the variables listed in Table 2.

Table 2. List of input variables that are used in this ATBD.

DP	Units		
Ultrasonic anemometer variables			
Time series (0.05 s temporal resolution) of the vertical wind component, perpendicular to mean streamline (w, AD[02])	m s ⁻¹		
Infrared gas analyzer variables			
Time series (0.05 s temporal resolution) of atmospheric scalar (X)	Depending on scalar		
Auxiliary variables			
Syncronization time lag (I_X)	s		
Individually for w and X , hard quality flag time series (0.05 s temporal resolution), indicating suitable ($QF_{hard} = 0$) or unsuitable ($QF_{hard} = 1$) measurement conditions (AD[03]).			
Individually for w and X , one hard quality metric flag per averaging period, indicating suitable or unsuitable measurement conditions (QM_{hard} , AD[03]).	%		



Author: S. Metzger

Date: 08/02/2013

NEON.DOC.000854

Revision: A

3.3 Product instances

Each NEON site with terrestrial infrastructure will produce an instance of the reported variables in Table 1.

3.4 Temporal resolution and extent

The temporal resolution of most reported variables in Table 1 is 0.05 s. Only the quality metric $QM_{\rm att}$ is reported only once per averaging period (0.5 h). The temporal extent of all reported variables is 0.5 h, i.e. the fundamental averaging period of DPs derived from the EC-TES. The temporal resolution of most input variables in Table 2 is 0.05 s. Only the quality metric $QM_{\rm hard}$ exists only once per averaging period (0.5 h). The temporal extent of all input variables is 0.5 h, i.e. a data set of 0.5 h duration shall be considered for each implementation of the presented algorithms.

3.5 Spatial resolution and extent

The input variables used in this ATBD are measured at a single position in space. Consequently both, input variables and reported variables are not spatially resolved. The spatial extent (path length) of all variables is ≈ 10 cm (AD[04]). The spatial representativeness of the variables reported in this ATBD is a function of several factors such as measurement height $d_{\rm z,m}$, displacement height $d_{\rm z,d}$, wind speed and direction, atmospheric stability and surface roughness (AD[05]). From dispersion modeling (e.g., Schmid, 1994, Vesala et al., 2008) it is found that $10(d_{\rm z,m}-d_{\rm z,d}) \lesssim d_{\rm x,FP90} \lesssim 100(d_{\rm z,m}-d_{\rm z,d})$, where $d_{\rm x,FP90}$ is the cross-wind integrated upwind extent from within which 90% of a measured flux value is sourced. The spatial representativeness for each observation of the reported variables will be quantified in the relevant ATBD (AD[01] provides an overview).

4 SCIENTIFIC CONTEXT

The intention of NEON EC-TES measurements is to determine the surface-air exchange of momentum, heat, water vapor and CO₂ from fast response measurements of the wind vector components, temperature, and scalar concentrations.

4.1 Theory of measurement/observation

The exchange of momentum, heat, water vapor, CO₂ and other scalars between the earth's surface and the atmosphere is mainly governed by turbulent transport. Buoyancy as well as shear stress result in a turbulent wind field for most of the day (e.g., Stull, 1988). The eddy-covariance (EC) technique measures the properties of the turbulent wind field directly. This makes it the least invasive method currently available for direct and continuous observations of the surface-air exchange. The technique is based on the concept of mass conservation and makes use of the Reynolds decomposition (isolation of mean and fluctuating part) of relevant terms in the Navier-Stokes equation (e.g., Foken, 2008, Stull, 1988). With



Author: S. Metzger

Date: 08/02/2013

NEON.DOC.000854 Revision: A

several restrictions (AD[01]) the net flux F into or out of an ecosystem can be expressed as (e.g., Loescher et al., 2006);

$$F = \int_{0}^{d_{z,m}} \frac{\partial \overline{X}}{\partial t} dz + \int_{0}^{d_{z,m}} \frac{\partial \overline{u'X'}}{\partial x} dz + \int_{0}^{d_{z,m}} \frac{\partial \overline{v'X'}}{\partial y} dz + \int_{0}^{d_{z,m}} \frac{\partial \overline{w'X'}}{\partial z} dz$$

$$= I \qquad \qquad II \qquad \qquad IV \qquad \qquad IV$$

$$+ \int_{0}^{d_{z,m}} \frac{\partial \overline{u}\overline{X}}{\partial x} dz + \int_{0}^{d_{z,m}} \frac{\partial \overline{v}\overline{X}}{\partial y} dz + \int_{0}^{d_{z,m}} \frac{\partial \overline{w}\overline{X}}{\partial z} dz,$$

$$V \qquad \qquad VI \qquad \qquad VII$$

$$(1)$$

with overbars denoting means, and primes denoting deviations from the mean. Here, X is a scalar quantity such as H_2O or CO_2 mixing ratios; u, v and w are along-, cross-, and vertical wind speeds with respect to the Cartesian coordinates x, y, and z; t is time, and $d_{z,m}$ is the measurement height. Term I in Eq. (1) represents the positive or negative rate of change of X in the vertical column below the sensor, equivalent to storage. Terms II–IV represent the turbulent flux divergence, and terms V–VII represent advection through the layer between the surface and sensor. If the conditions at the measurement site fulfill several assumptions (details provided in AD[01]), terms I–III and V–VII cancel from Eq. (1), and term IV can be further simplified to;

$$F = \overline{w'X'}. (2)$$

That is, in this case the net flux into or out of an ecosystem can be expressed as the covariance between the vertical wind and the scalar, which can be computed from EC-TES measurements alone. Whether or not this reduction of Eq. (1) is valid will be assessed in a series of tests during the implementation of AD[01]. Wherever possible, auxiliary measurements will be used to re-substitute non-negligible terms in Eq. (2), e.g. the storage term I (AD[06]).

4.2 Theory of algorithm

EC measurement systems, like all measuring instruments, act as filters, removing both high- and low-frequency components of a signal. High-frequency losses are mainly due to inadequate sensor frequency response, line averaging, sensor separation and, in closed-path infrared gas analyzer (IRGA) systems, air transport through a filter and a tube (Foken et al., 2012). Figure 1 schematically illustrates the impact of high frequency loss in the measurement of an atmospheric scalar X, such as CO_2 or H_2O dry mole fraction, on spectral density (The calculation of power spectra are detailed in AD[07]). The frequency range of attenuation depends on the instrumental setup and especially the length and conditioning of the sample tube. It is often confined to frequencies beyond the spectral peak, which is referred to as the inertial subrange (ISR) of atmospheric turbulence. As can be seen from Eq. (2), high frequency losses in X



Author: S. Metzger

Date: 08/02/2013

NEON.DOC.000854

Revision: A

propagate into the EC-TES flux measurement, and the corresponding cospectrum CO(w,X). Low-frequency losses result from the finite sampling duration, with the averaging period not always being sufficiently long to include all relevant low frequencies. The subject of this ATBD is the correction of high-frequency losses, in order to avoid underestimating the variances and covariances of outputs from EC-TES sensors (up to 20%, Nordbo and Katul, 2012, AD[03]). Low-frequency losses are not subject of this ATBD, and will be addressed in a series of tests during the implementation of AD[01].

Until recently, two general approaches have been used to correct the effect of high-frequency attenuation of EC instruments on the measured fluxes. In the theoretical approach, the transfer function TF(w,X) is deduced from prior knowledge of the measuring system and a theoretical cospectral density function (e.g., Horst and Lenschow, 2009, Moore, 1986). In the experimental approach, TF(w,X) is calculated from the ratio of two simultaneously measured cospectra (e.g., Fratini et al., 2012, Runkle et al., 2012). In this approach one cospectrum refers to the filtered scalar of interest, and the other is considered as a reference and supposedly real cospectrum. In practice, the sensible heat cospectrum is usually used as reference (Foken et al., 2012).

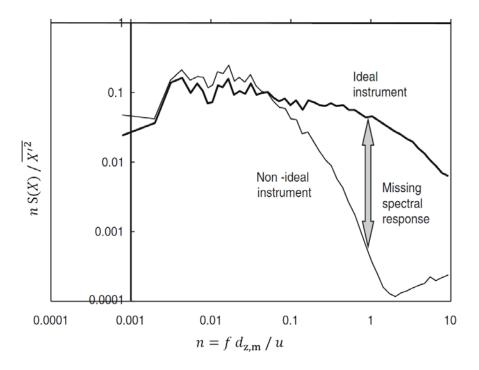


Figure 1. Modified after Foken et al. (2012): Normalized power spectrum for an ideal instrument which measures the unaffected spectrum of turbulence, and for a non-ideal instrument. The missing energy between both response curves must be corrected (normalized frequency n; measurement frequency f, measurement height $d_{z,m}$, along-wind speed u, power spectrum and variance of atmospheric scalar X, S(X) and $\overline{X'}^2$, respectively). The calculation of power spectra are detailed in AD[07].



Author: S. Metzger

Date: 08/02/2013

NEON.DOC.000854 Revision: A

The theoretical approach has the advantage of relying on a fundamental description of the system and allows a comprehensive description of filtering processes. Its shortcomings are; (i) the theoretical cospectral densities not necessarily correspond to the real cospectral densities observed at the sites (e.g., De Ligne et al., 2010), (ii) a static transfer function cannot accommodate transient changes in a closed-path IRGA system, such as in the tube flow regime with ambient temperature, or in the adsorption/desorption behavior of the intake tube or the particle filter with accumulating dirt. While well suited for open-path IRGAs, the application of the theoretical approach to closed-path IRGA systems appears more difficult (Foken et al., 2012).

The experimental approach assumes that; (i) the high-frequency attenuation of sensible heat cospectral density is negligible compared with those affecting other tracers, and (ii) the processes of atmospheric turbulent transport of sensible heat and other tracers are similar and therefore the cospectral densities should be proportional to each other. The former assumption makes sense for closed-path systems where high-frequency losses are mainly resulting from tube or filter attenuation. In open-path systems however, the experimental approach could lead to an underestimation of the high-frequency correction (Foken et al., 2012). The second assumption, scalar similarity, generally holds true for the high-frequency part of the spectrum under daytime conditions. However, variations have been observed among scalars, as well as between different times of the day (Ruppert et al., 2006).

In order to combine the strengths of the theoretical and the empirical approaches, site-specific calibrations of the theoretical transfer functions have been derived (e.g., De Ligne et al., 2010, Spank and Bernhofer, 2008). Nevertheless, all of the forenamed approaches (i) are limited to correcting the resulting covariance Eq. (2) but do not restore the high-frequency data itself, and (ii) cannot easily be fully automated.

More recently Nordbo and Katul (2012, in the following referred to as NK12) have presented a novel approach to high frequency spectral corrections which (i) directly corrects the high-frequency data instead of the cospectrum, (ii) corrects each individual averaging period, and is thus able to take into account variations in environmental conditions (e.g., flow rate, relative humidity), (iii) does not assume cospectral similarity with heat, and (iv) does not rely on a theoretical shape for the velocity–scalar cospectrum, thereby making it advantageous to employ in non-ideal conditions. Furthermore, the method is not gas specific, and can be used with very little input information at various sites. The method's largest insufficiency is its inability to correct attenuation starting already near the peak of power spectra, which however is explicitly taken into account in the design of NEON's EC-TES. Consequently this is the method of choice for NEON, as it overcomes the drawbacks of the conventional approaches, and is fully automatable. Cospectral attenuation through sensor separation is not considered by the NK12 method. Instead it is explicitly addressed in AD[03] through maximization of the cross-correlation and by using an exponential decay model. Sect. 4.2.1 provides an overview of the NK12 method, including an outline of assumptions and idealizations. In Sects. 4.2.2–4.2.7 a detailed sequence of algorithmic steps is presented.



Author: S. Metzger

Date: 08/02/2013

NEON.DOC.000854

Revision: A

4.2.1 Wavelet-based spectral correction method

The NK12 method uses the time-frequency localities of orthonormal wavelets to adjust high frequency time series prior to the computation of any turbulence statistics. It resembles a transfer-function method, because lost variance is recreated using a power spectral model. However, instead of only correcting variance loss, the procedure in the wavelet half-plane also enables correcting travel time distortions, e.g. resulting from tube wall effects. The NK12 method poses the following assumptions;

- (i) The peak of S(w) occurs at frequencies that are higher than the peak of S(X);
- (ii) The variance loss in X occurs at frequencies that are higher than the peak frequency of S(w);
- (iii) S(X) possesses a power-law decay in the ISR.

These assumptions are relatively weak compared to those of the conventional approaches. Moreover, assumption (ii) can be taken into consideration in the design process of an EC system, and assumptions (i) and (iii) are supported by experimental findings under a broad variety of environmental conditions (Kaimal and Finnigan, 1994 provide a comprehensive summary). Figure 2 gives an overview of the NK12 spectral correction method consisting of the following subsequent steps;

- (i) In Sect. 4.2.2 a discrete wavelet transform is performed on w and X, and their wavelet power spectra are determined;
- (ii) In Sect. 4.2.3 the spectral peak n_{\max} of the w power spectrum is determined. It is preconditioned that the scalar power spectrum S(X) is not attenuated for frequencies $n(S(X)) \le n_{\max}(S(w))$, and spectral correction is only required for frequencies $n(S(X)) > n_{\max}(S(w))$;
- (iii) In Sect. 4.2.4 the slope of the power-law decay in the ISR is determined from regression over S(X) in the frequency range that falls within the ISR and fulfills the condition $n(S(X)) \le n_{\max}(S(w))$. For each frequency in the range $n(S(X)) > n_{\max}(S(w))$ the required amplitude adjustment for S(X) is determined as the difference of the extrapolated power-law slope and S(X);
- (iv) In Sect. 4.2.5 only those wavelet coefficients of *X* are selected which coincide with high energy in the wavelet coefficients of *w*;



Author: S. Metzger

Date: 08/02/2013

NEON.DOC.000854 Revision: A

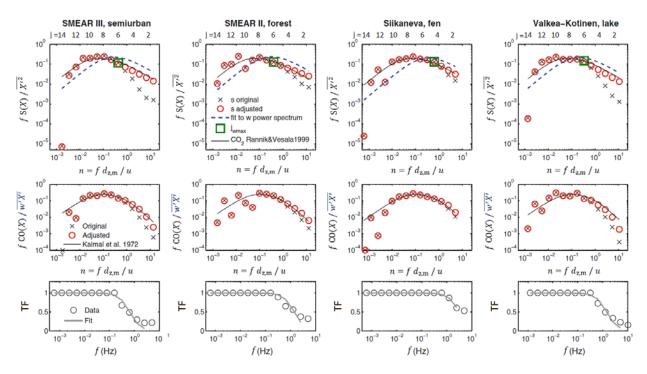


Figure 2. Modified after Nordbo and Katul (2012): Overview of the wavelet-based spectral correction method for four case studies. Top row: power spectra as function of the normalized frequency n (original with black crosses; adjusted with red circles). A fit to the power spectrum of w (blue dashed line) is used to derive the frequency limit $n_{\text{max}}(S(w))$ (green square). Atop the plot the scale indices j of the data points are displayed. Middle row: cospectra as a function of n (original with black crosses; adjusted with red circles) and the reference cospectrum of Kaimal et al. (1972) for comparison. Bottom row: deduced transfer function (TF) as a function of the natural frequency f.

- (v) In Sect. 4.2.6 the required amplitude adjustment is performed for the selected wavelet coefficients of *X*;
- (iv) In Sect. 4.2.7 the corrected scalar time series is reconstructed from the unmodified and adjusted wavelet coefficients in the frequency ranges $n(S(X)) \le n_{\max}(S(w))$ and $n(S(X)) > n_{\max}(S(w))$, respectively. This is achieved by an inverse wavelet transform.

4.2.2 Discrete wavelet transform

In wavelet analysis, a time series is decomposed into a set of small pulses of a predefined shape. Unlike Fourier transforms, wavelet transforms do not only retain the scale (inverse proportional to frequency) and amplitude information of a pulse, but also its location in time. Here a discrete wavelet transform is used, with an orthonormal wavelet basis and dyadically (powers of two) arranged scales. Details on the reasoning of this choice are provided by NK12, who define the discrete wavelet convolution as;



Author: S. Metzger

Date: 08/02/2013

NEON.DOC.000854

Revision: A

$$W_{j}[i] = \sum_{i=1}^{2^{J-j}} g_{j}[i-2^{j}t] Y[t], \tag{3}$$

where $W_j[i]$ is the wavelet coefficient (amplitude of variation) at scale index $j \in \{1...J\}$ and location index $i \in \{1...Z^{j-j}\}$, g_j is a discrete wavelet, and Y[t] is the time series of $Y \in \{X, w\}$, with the time position index t. In other words, if we have an EC raw data record of length $2^{15} = 32768$, then J = 15 different eddy sizes are resolved, each described by the unique scale index j. The number of wavelet coefficients for each scale index j is expressed by 2^{J-j} , ranging from $2^{15-15} = 2^0 = 1$ for the largest scale to $2^{15-1} = 2^{14}$ for the smallest scale, with an overall number of 2^J-1 wavelet coefficients. Figure 3 shows a schematic illustration of the resulting scale vs. location representation of Y in the wavelet half-plane.

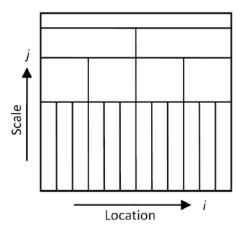


Figure 3. Relation of the resolution of location (index i) and scale (index j) for the discrete wavelet transform.

NK12 select the Haar Wavelet for the forward and backward transforms;

$$g(t) \begin{cases} 1 & 0 \le t \le 1/2 \\ -1 & 1/2 \le t \le 1 \\ 0 & \text{otherwise} . \end{cases}$$
 (4)

In the wavelet transform, g is dilated (i.e. stretched) to match a scale of variation, and translated to correspond to a time location in Y. The variation frequency f_j and the normalized variation frequency n_j can be calculated for each scale index j as;

$$f_{\mathbf{j}} = \frac{2^{J-j}}{2^J} f,\tag{5}$$

$$n_{\rm j} = \frac{d_{\rm z,m}}{\overline{u}} f_{\rm j},\tag{6}$$



Author: S. Metzger

Date: 08/02/2013

NEON.DOC.000854

Revision: A

with sampling frequency f, measurement height $d_{z,m}$ and the average along-wind speed for a given averaging period \bar{u} . The wavelet variance $\overline{Y'^2}$ (overbars and primes denote averages and immediate deviations from the average, respectively) is the mean of the squared wavelet coefficients over all scale and location indices;

$$\overline{Y'^2} = \frac{1}{2J} \sum_{j=1}^{J} \sum_{i=1}^{2J-j} (W_j[i])^2.$$
 (7)

The NK12 spectral correction method commences by computing the normalized wavelet power spectrum $S_n(Y)$ with $Y \in \{X, w\}$;

$$S_{n,j}(Y) = f \frac{S_j(Y)}{\overline{Y'^2}} = \frac{f_j}{f} \frac{\overline{W_j^2}}{\overline{Y'^2} \ln(2)} = \frac{2^{J-j}}{2^J} \frac{\overline{W_j^2}}{\overline{Y'^2} \ln(2)},$$
(8)

with the function of the natural logarithm In(). The normalized wavelet power spectrum before correction and its scale indices are shown in Figure 2 (black crosses, NK12). For more information on wavelet analysis, NK12 provide a comprehensive reference list.

4.2.3 Spectral peaks

A 100-point fit to the power spectrum (blue dashed line in Figure 2, top row) is used to determine the frequency $j_{max}(w)$ at which the peak in $S_n(w)$ occurs (green square in Figure 2, top row). The Wavelet coefficients $W_j(X)$ for which $j < j_{max}(w)$ are assumed to potentially require adjustment for high frequency spectral loss (e.g., scale indices 5–1 in Figure 2, top row, SMEAR III, NK12).

4.2.4 Power law coefficient in the inertial subrange

The Wavelet coefficients $W_j(X)$ for which scale index $j_{max}(w)-2 \le j \le j_{max}(w)$ are used to determine how much $W_j(X)$ at smaller scale indices $(j < j_{max}(w))$ are to be adjusted (e.g., scale indices 6-8 in Figure 2, top row, SMEAR III). Obtaining the ISR power law coefficient from scale indices $j_{max}(w)-2 \le j \le j_{max}(w)$ is based on the argument that e.g. tube effects do not attenuate the lower frequencies residing in the ISR. The un-attenuated log-log scale slope (power law coefficient) in the inertial subrange of S(X) is obtained from least-squares regression over $S_j(X)$ for scale indices $j_{max}(w)-2 \le j \le j_{max}(w)$. If the regression slope falls within -1.8...-1.3 it will be deemed as plausible and used for extrapolation to obtain the un-attenuated power at smaller scale indices $(j < j_{max}(w))$. The bounds -1.8...-1.3 are conservatively chosen to accommodate effects such as intermittency or wakes that may cause anomalous departures from the -5/3 law of isotropic turbulence in the ISR. If the departure however exceeds the bounds -1.8...-1.3, the conventional -5/3 slope is used as a logical alternative (NK12).



Author: S. Metzger

Date: 08/02/2013

NEON.DOC.000854 Revision: A

4.2.5 Distribution of amplitude adjustment

In the theoretical and the experimental approaches, high-frequency attenuation is compensated by adjusting the cospectral energy for each averaging interval, irrespective of within-averaging interval variations. In reality however, e.g. tube wall effects do not only attenuate the amplitude of a signal, but also distort (or smear) its travel-time. In the Wavelet half-plane, travel-time distortions show as smeared spectral energy along the locations of the wavelet coefficients, and can be addressed explicitly. That is, some spectral energy is attributed to wavelet coefficients that should not have energy, and thus should also not be amplified. To compensate this distortion, only those scalar wavelet coefficients $W_j(X)[i]$ are adjusted for which the corresponding wavelet coefficients of the vertical wind $W_j(w)[i]$ are sufficiently energetic. The criterion used here is that $\left(W_j(w)[i]\right)^2$ has to be among the largest coefficients that contribute to 90% of the local scale-wise total energy. That is, for each scale index $j < j_{\text{max}}(w)$ for which $W_j(X)$ needs to be adjusted, a subgroup of position indices i_c is selected for correction, and another subgroup of position indices i_c remains unaltered (NK12).

4.2.6 Correction for high-frequency loss

Now that the scale and position indices of the wavelet coefficients to be adjusted are known, the amplitude adjustment can be made. (i) the corrected amplitudes $A_{j,c}(X) = \sqrt{S_{j,c}(X)}$ are calculated for each scale in the potentially attenuated range of scale indices $j < j_{\text{max}}(w)$. This is achieved by extrapolating the ISR log-log scale slope (determined in Sect. 4.2.4) into the range of scale indices $j < j_{\text{max}}(w)$, resulting in $S_{j,c}(X)$. (ii) The dimensionless amplification energy in each scale E_j is found from the ratio between the un-attenuated amplitudes and the attenuated amplitudes. A weighting procedure is used to take into account that only a selected fraction of all wavelet coefficients for a given scale are adjusted;

$$E_{j} = \left(\frac{A_{j,c}}{A_{i,c}}\right)^{2} \frac{\overline{W_{j}^{2}[\iota_{c},\iota_{0}]} \, N(i_{c},i_{0}) - \overline{W_{j}^{2}[\iota_{0}]} \, N(i_{0})}{\overline{W_{j}^{2}[\iota_{c}]} \, N(i_{c})},\tag{9}$$

with $N(i_0)$ and $N(i_c)$ being the number of wavelet coefficients that remain unaltered and those that are selected for correction, respectively, and $N(i_0,i_c) = N(i_0) + N(i_c)$. The fraction $A_{j,c}/A_j$ is not allowed to be below unity, i.e. the correction cannot dampen wavelet coefficients. The corrected wavelet coefficients are then given as;

$$W_{j,c}[i_c] = W_j[i_c] \sqrt{E_j}. \tag{10}$$

Thus, the amplitude adjustment is completely based on the time-localization feature of wavelets, though E_i stays the same for a certain scale (NK12).



Author: S. Metzger

Date: 08/02/2013

NEON.DOC.000854

Revision: A

4.2.7 Reconstruction of the corrected time series

Lastly, the corrected time series of X, X_c , is reconstructed by performing an inverse wavelet transform over unadjusted $W_j(X)$ at larger scale indices $(j \ge j_{\max}(w))$ and adjusted $W_{j,c}(X)$ at smaller scale indices $(j < j_{\max}(w))$.

5 ALGORITHM IMPLEMENTATION

The implementation of Eqs. (3)–(10) is organized in three steps, which also include the consideration of previously determined data quality flags and metrics (AD[03]);

- (i) If more than 10% of the observations of either w or X are rendered unsuitable (respective quality metric $QM_{hard} > 10\%$), no correction is performed, and the algorithm stops here (Mauder and Foken, 2011). X is assigned to X_c , and the corresponding averaging period is assigned a quality metric $QM_{att} = 100\%$, indicating that no correction for spectral loss could be performed.
- (ii) If $QM_{hard} \le 10\%$ for both w and X, shift X by I_X with respect to w to offset the decorrelation effect of along-wind sensor separation. Discard observations of w and X with respective quality flag $QF_{hard} = 1$. Perform a linear interpolation over the time series of w and X to fill the missing values. This procedure solely facilitates correcting high-frequency spectral loss for all suitable observations (respective quality flag $QF_{hard} = 0$). For this purpose continuous data sets of w and X with all artifacts removed are required. However, the interpolated data points are not used for the calculation of means, variances or covariances from EC-TES variables (AD[03]).
- (iii) De-trend both w and X, and perform Eqs. (3)–(10) as implemented in detail for a test dataset in the NK12 source code (AD[08]). Assign a quality metric $QM_{\rm att}$ = 0% to the corresponding averaging period.

 X_c and QM_{att} shall be reported as results of this ATBD, i.e. they shall be made available as input variables for subsequent ATBDs (Table 1).

6 UNCERTAINTY

This section concerns only the propagation of sensor/calibration uncertainty in the input variables, through the presented algorithms, into the variables reported in this ATBD. This section does not concern testing the fulfillment of assumptions in the EC method, quantification of sampling errors and the like. These sources of uncertainty are addressed in a series of tests during the implementation of AD[01] (details provided therein).

Once all higher-level NEON DPs are mapped out, an integrated uncertainty propagation plan will be derived. At the present time this section represents a simplified indicator for the potential direction of



Author: S. Metzger

Date: 08/02/2013

NEON.DOC.000854

Revision: A

such uncertainty propagation plan. For this purpose resolution is defined as the smallest detectable change in a variable, and accuracy and precision are defined as the systematic and random uncertainties in a variable, respectively. In the following sections, generic algorithms are provided that enable the propagation of resolution, accuracy and precision through Eqs. (3)–(10).

6.1 Analysis of uncertainty

Following Taylor (1997) the maximum probable error σ_A of a function F with N input variables (X) is defined as;

$$\sigma_{\mathcal{A}}(F) = \sum_{i=1}^{N} \left| \frac{\partial F}{\partial X_i} \right| \sigma_{\mathcal{A}}(X_i). \tag{11}$$

The partial derivative $\partial F/\partial X_i$ is the slope of F with X_i , and hence quantifies the sensitivity of F on uncertainty in X_i . In the following, Eq. (11) is used as model for the propagation of accuracy (subscript A) through Eqs. (3)–(10). If random and independent, the uncertainties in X_i tend to cancel, and Gaussian quadrature applies;

$$\sigma_{\rm P}^2({\rm F}) = \sum_{i=1}^N \left(\frac{\partial {\rm F}}{\partial X_i} \sigma_{\rm P}(X_i) \right)^2. \tag{12}$$

Eq. (12) is used as the model for the propagation of precision (subscript P) and resolution through Eqs. (3)–(10). At this point, it is assumed that the resolution follows a binomial distribution (low amplitude noise between two adjacent discrete values, Vickers and Mahrt, 1997). For sufficiently large sample sizes (20 or greater, Box et al., 2005), the binomial distribution is reasonably approximated by the normal distribution, and can be quantified by Gaussian metrics such as Eq. (12).

6.2 Reported uncertainty

In order to calculate the accuracy, precision and resolution for each reported variable in Table 1, the partial derivatives of Eqs. (3)–(10) shall be found, and combined in accordance with Eqs. (11)–(12). Eq. (12) analogously applies for the determination of the resulting resolution, when replacing the precisions (standard deviations) σ_P with the resolutions (finite differences) Δ_R .

7 ALGORITHM VERIFICATION

Verification of the algorithms disclosed in this ATBD shall follow the procedures outlined in AD[09]. During the implementation of AD[01], DPs will be derived from the present algorithms, and DP verification and validation will be specified accordingly.



Title: NEON	Algorithm	Theoretical	Basis	Document -
Frequency R	acnonca Co	rrections		

Date: 08/02/2013

NEON.DOC.000854

Revision: A

8 SCIENTIFIC AND EDUCATIONAL APPLICATIONS

The correction of high-frequency spectral loss is the basis to confidently process EC turbulence data into higher-level DPs with ecological relevance. The present ATBD details all relevant transformations as well as the propagation of uncertainty through these transformations. During the implementation of AD[01], data will continue to be processed into higher-level DPs. Ecologically relevant high-level DPs of the ECTES include the exchange of heat, water vapor and CO₂ between the land surface and the atmosphere. These DPs are used for constraining, calibrating and validating process-based models (e.g., Rastetter et al., 2010). This shall enable the detection of continental scale ecological change and the forecasting of its impacts.

Standardized and transparent documentation intends to foster reproducibility of all data processing steps. For this purpose, it is planned to make all processing steps available as open-source code in a high-level programming language. Aside from enabling direct feedback from the research community, this also provides community members (e.g. students at graduate level) a straightforward and hands-on toolbox for data processing of micrometeorological measurements.

9 FUTURE PLANS AND MODIFICATIONS

This ATBD will be version controlled, i.e. future developments might results in modifications to this ATBD, which will be documented accordingly.

10 APPENDIX

10.1 Acronyms

Acronym	Description
ATBD	Algorithm theoretical basis document
C ³	Command, control, and configuration document
CO ₂	Carbon dioxide
DP	Data product
EC	Eddy covariance
EC-TES	Eddy-covariance turbulent exchange subsystem
FFT	Fast Fourier transform
FIU	Fundamental instrument unit (NEON project team)



Title: NEON Algorithm Theoretical Basis Document -
Frequency Response Corrections

Date: 08/02/2013

Revision: A

NEON.DOC.000854

Acronym	Description
H₂O	Water vapor
IRGA	Infrared gas analyzer
NEON	National Ecological Observatory Network
NK12	Nordbo, A. & Katul, G. (2012) A wavelet-based correction method for eddy-covariance high-frequency losses in scalar concentration measurements. <i>Boundary-Layer Meteorology</i> , 146 , 81-102.
QA/QC	Quality Assurance/Quality Control

10.2 Functions

Function	Description
[]	Position index
СО	Cospectrum
9	Partial differential operator
Δ	Finite difference operator
∈{ <i>X, Y</i> }	Element of a set that includes X and Y
F	Function for error propagation
In	Natural logarithm
S	Power spectrum
σ	Standard deviation
TF	Transfer function
\bar{X}	Short-term (e.g., 30 min) arithmetic mean of atmospheric quantity <i>X</i>
$\overline{X'X'}, \overline{X'^2}$	Short-term (e.g., 30 min) sample variance of atmospheric quantity X
$\overline{X'Y'}$	Short-term (e.g., 30 min) sample covariance of atmospheric quantities <i>X</i> and <i>Y</i>



Author: S. Metzger

Date: 08/02/2013

NEON.DOC.000854

Revision: A

10.3 Parameters

Parameter	Description	Numeric value	Units
J	Sample size	User-defined	Dimensionless (count)
N	Sample size	User-defined	Dimensionless (count)

10.4 Subscripts

Subscript	Description
1 <i>N</i>	Numeric identifier
Α	Accuracy
С	Corrected
hard	Measurement or instrument conditions that do not permit data usage
i	Running index
j	Running index
m	Measurement
max	Maximum
n	Normalized
Р	Precision
R	Resolution
X, Y	Placeholder for atmospheric quantities
х, у, z	Along-, cross- and vertical axes of a Cartesian coordinate system



NEON.DOC.000854

Author: S. Metzger

Date: 08/02/2013

Revision: A

10.5 Variables

Variable	Description	Units	
Α	Amplitude	Depending on use case	
d	Distance/length/height	m	
d _{x,FP90}	Cross-wind integrated upwind extent from within which 90% of an observed value is sourced	m	
$d_{z,d}$	Displacement height	m	
E	Energy	Depending on use case	
f	Frequency	Hz	
F	Flux into or out of an ecosystem	Depending on unit of scalar	
i	Running index	Dimensionless (count)	
j	Running index	Dimensionless (count)	
1	Lag time	S	
n	Normalized frequency	Dimensionless	
QF	Quality flag	Dimensionless (0 or 1)	
QM	Quality metric (same subscripts as for QF apply)	%	
t	Time	S	
u, v, w	Along-, cross- and vertical wind speed	m s ⁻¹	
x, y, z	Along-, cross- and vertical axes of a Cartesian coordinate system	Dimensionless	
<i>X, Y</i>	Placeholder for atmospheric quantities	Depending on unit of atmospheric quantity	



Author: S. Metzger

Date: 08/02/2013

NEON.DOC.000854 Revision: A

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Title: NEON	Algorithm '	Theoretical	Basis	Document -
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Date: 08/02/2013

NEON.DOC.000854

Revision: A

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